

1997 Semester 1 Multiple Choice

2. If $f(x) = x\sqrt{2x-3}$, then $f'(x) =$

- (A) $\frac{3x-3}{\sqrt{2x-3}}$
- (B) $\frac{x}{\sqrt{2x-3}}$
- (C) $\frac{1}{\sqrt{2x-3}}$
- (D) $\frac{-x+3}{\sqrt{2x-3}}$
- (E) $\frac{5x-6}{2\sqrt{2x-3}}$

4. If $f(x) = -x^3 + x + \frac{1}{x}$, then $f'(-1) =$

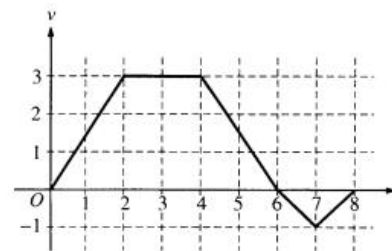
- (A) 3
- (B) 1
- (C) -1
- (D) -3
- (E) -5

5. The graph of $y = 3x^4 - 16x^3 + 24x^2 + 48$ is concave down for

- (A) $x < 0$
- (B) $x > 0$
- (C) $x < -2$ or $x > -\frac{2}{3}$
- (D) $x < \frac{2}{3}$ or $x > 2$
- (E) $\frac{2}{3} < x < 2$

7. $\frac{d}{dx} \cos^2(x^3) =$

- (A) $6x^2 \sin(x^3) \cos(x^3)$
- (B) $6x^2 \cos(x^3)$
- (C) $\sin^2(x^3)$
- (D) $-6x^2 \sin(x^3) \cos(x^3)$
- (E) $-2 \sin(x^3) \cos(x^3)$



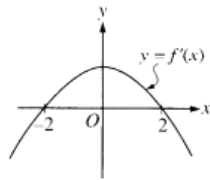
A bug begins to crawl up a vertical wire at time $t = 0$. The velocity v of the bug at time t , $0 \leq t \leq 8$, is given by the function whose graph is shown above.

8. At what value of t does the bug change direction?

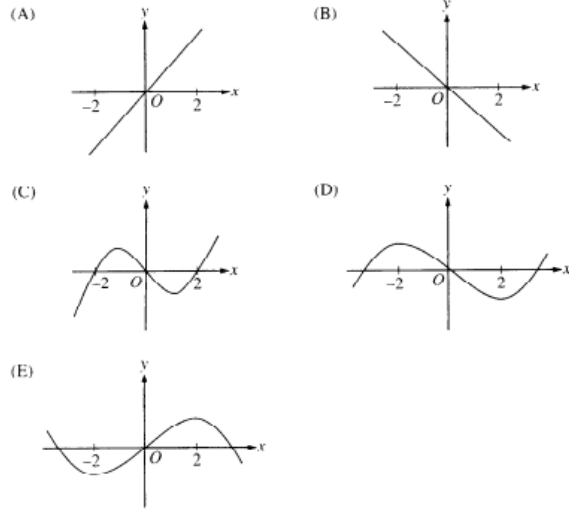
- (A) 2
- (B) 4
- (C) 6
- (D) 7
- (E) 8

10. An equation of the line tangent to the graph of $y = \cos(2x)$ at $x = \frac{\pi}{4}$ is

- (A) $y - 1 = -\left(x - \frac{\pi}{4}\right)$
- (B) $y - 1 = -2\left(x - \frac{\pi}{4}\right)$
- (C) $y = 2\left(x - \frac{\pi}{4}\right)$
- (D) $y = -\left(x - \frac{\pi}{4}\right)$
- (E) $y = -2\left(x - \frac{\pi}{4}\right)$



11. The graph of the derivative of f is shown in the figure above. Which of the following could be the graph of f ?



12. At what point on the graph of $y = \frac{1}{2}x^2$ is the tangent line parallel to the line $2x - 4y = 3$?

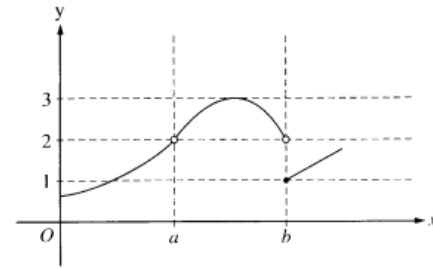
- (A) $\left(\frac{1}{2}, -\frac{1}{2}\right)$ (B) $\left(\frac{1}{2}, \frac{1}{8}\right)$ (C) $\left(1, -\frac{1}{4}\right)$ (D) $\left(1, \frac{1}{2}\right)$ (E) $(2, 2)$

13. Let f be a function defined for all real numbers x . If $f'(x) = \frac{|4-x^2|}{x-2}$, then f is decreasing on the interval

- (A) $(-\infty, 2)$ (B) $(-\infty, \infty)$ (C) $(-2, 4)$ (D) $(-2, \infty)$ (E) $(2, \infty)$

14. Let f be a differentiable function such that $f(3) = 2$ and $f'(3) = 5$. If the tangent line to the graph of f at $x = 3$ is used to find an approximation to a zero of f , that approximation is

- (A) 0.4 (B) 0.5 (C) 2.6 (D) 3.4 (E) 5.5



15. The graph of the function f is shown in the figure above. Which of the following statements about f is true?

- (A) $\lim_{x \rightarrow a} f(x) = \lim_{x \rightarrow b} f(x)$
 (B) $\lim_{x \rightarrow a} f(x) = 2$
 (C) $\lim_{x \rightarrow b} f(x) = 2$
 (D) $\lim_{x \rightarrow b} f(x) = 1$
 (E) $\lim_{x \rightarrow a} f(x)$ does not exist.

17. If $x^2 + y^2 = 25$, what is the value of $\frac{d^2y}{dx^2}$ at the point $(4, 3)$?

- (A) $-\frac{25}{27}$ (B) $-\frac{7}{27}$ (C) $\frac{7}{27}$ (D) $\frac{3}{4}$ (E) $\frac{25}{27}$

19. If $f(x) = \ln|x^2 - 1|$, then $f'(x) =$

- (A) $\frac{2x}{x^2 - 1}$
 (B) $\frac{2x}{|x^2 - 1|}$
 (C) $\frac{2|x|}{x^2 - 1}$
 (D) $\frac{2x}{x^2 - 1}$
 (E) $\frac{1}{x^2 - 1}$

21. $\lim_{x \rightarrow 1} \frac{x}{\ln x}$ is
- (A) 0 (B) $\frac{1}{e}$ (C) 1 (D) e (E) nonexistent

22. What are all values of x for which the function f defined by $f(x) = (x^2 - 3)e^{-x}$ is increasing?
- (A) There are no such values of x .
(B) $x < -1$ and $x > 3$
(C) $-3 < x < 1$
(D) $-1 < x < 3$
(E) All values of x

Graphing Calculator Allowed

76. If $f(x) = \frac{e^{2x}}{2x}$, then $f'(x) =$
- (A) 1
(B) $\frac{e^{2x}(1-2x)}{2x^2}$
(C) e^{2x}
(D) $\frac{e^{2x}(2x+1)}{x^2}$
(E) $\frac{e^{2x}(2x-1)}{2x^2}$
77. The graph of the function $y = x^3 + 6x^2 + 7x - 2 \cos x$ changes concavity at $x =$
- (A) -1.58 (B) -1.63 (C) -1.67 (D) -1.89 (E) -2.33
79. Let f be a function such that $\lim_{h \rightarrow 0} \frac{f(2+h) - f(2)}{h} = 5$. Which of the following must be true?
- I. f is continuous at $x = 2$.
II. f is differentiable at $x = 2$.
III. The derivative of f is continuous at $x = 2$.
- (A) I only (B) II only (C) I and II only (D) I and III only (E) II and III only

80. Let f be the function given by $f(x) = 2e^{4x^2}$. For what value of x is the slope of the line tangent to the graph of f at $(x, f(x))$ equal to 3?
- (A) 0.168 (B) 0.276 (C) 0.318 (D) 0.342 (E) 0.551
81. A railroad track and a road cross at right angles. An observer stands on the road 70 meters south of the crossing and watches an eastbound train traveling at 60 meters per second. At how many meters per second is the train moving away from the observer 4 seconds after it passes through the intersection?
- (A) 57.60 (B) 57.88 (C) 59.20 (D) 60.00 (E) 67.40
82. If $y = 2x - 8$, what is the minimum value of the product xy ?
- (A) -16 (B) -8 (C) -4 (D) 0 (E) 2
85. If the derivative of f is given by $f'(x) = e^x - 3x^2$, at which of the following values of x does f have a relative maximum value?
- (A) -0.46 (B) 0.20 (C) 0.91 (D) 0.95 (E) 3.73